

GRAPHING LOGS

Graphing form of a log function

$$y = a \cdot \log_2(x - h) + k$$

Equation of the asymptote = $x = h$

Locator Point = $(1, 0)$

2nd point = (base, 1)

Domain: $x > 0$

Range: \mathbb{R}

ex: Graph

$$y = \log_2(x + 3) - 1$$

Domain: $x > -3$

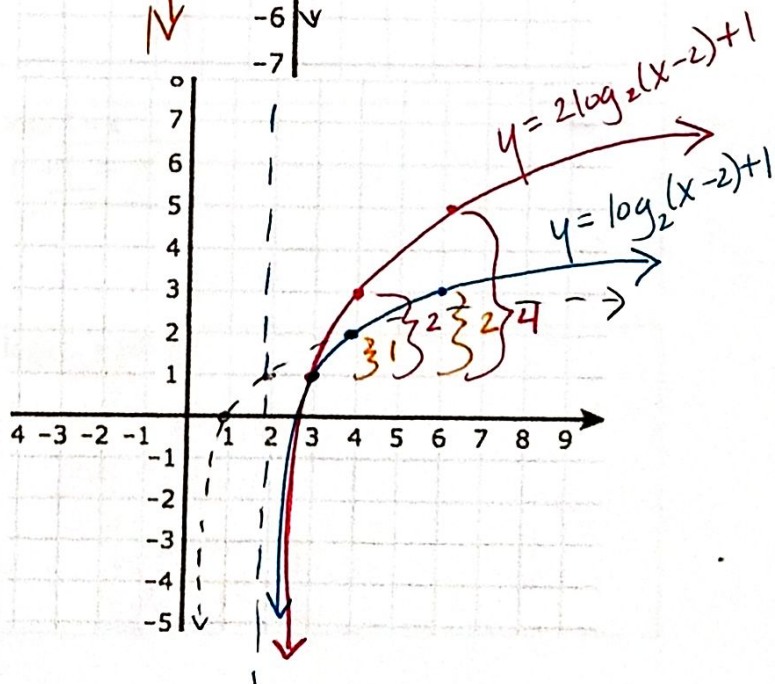
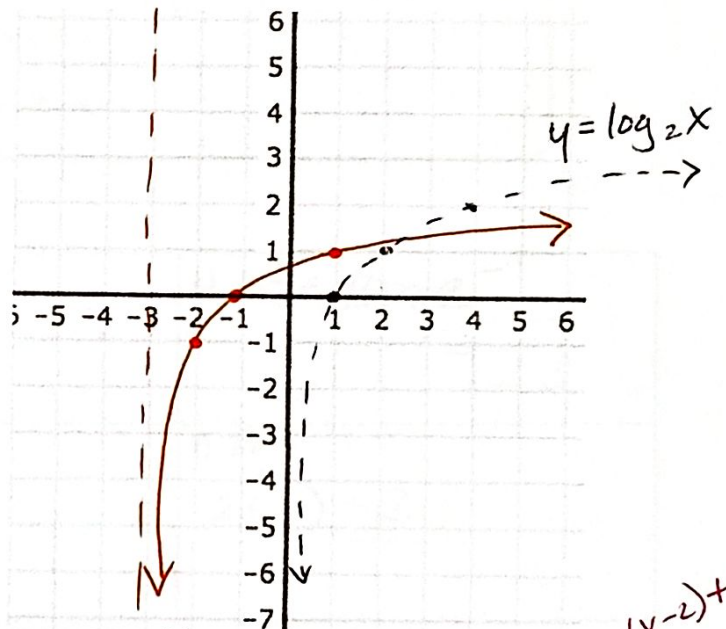
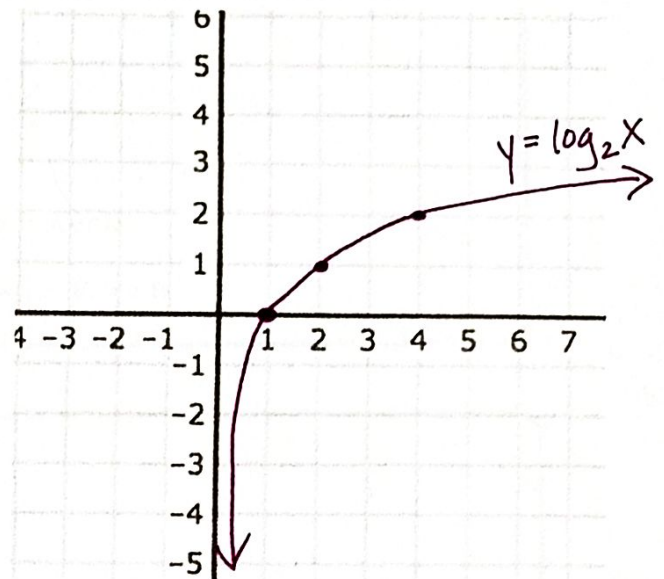
Range: \mathbb{R}

ex: Graph

$$y = 2 \cdot \log_2(x - 2) + 1$$

Domain: $x > 2$

Range: \mathbb{R}



PROPERTIES OF LOGS *PART 1*

Properties of Logarithms

- $\log_a 1 = 0$ because $a^0 = 1$.
- $\log_a a = 1$ because $a^1 = a$.
- $\log_a a^x = x$ and $a^{k \log_a x} = x$. Inverse Properties
- If $\log_a x = \log_a y$, then $x = y$. One-to-One Property

Properties of Natural Logarithms

- $\ln 1 = 0$ because $e^0 = 1$.
- $\ln e = 1$ because $e^1 = e$.
- $\ln e^x = x$ and $e^{\ln x} = x$. Inverse Properties
- If $\ln x = \ln y$, then $x = y$. One-to-One Property

Use Properties of Logs to simplify the following:

a) $\log_7 7^x = \boxed{x}$	b) $8^{\log_8 24} = \boxed{24}$	c) $\ln \frac{1}{e} = \ln e^{-1} = \boxed{-1}$
d) $e^{\ln 5} = \boxed{5}$	e) $4 \ln 1 = 4(0) = \boxed{4}$	f) $2 \ln e = 2(1) = \boxed{2}$

Use Properties of Logs to solve the following:

a) $\log_2(y) = \log_2(3)$ $\boxed{x = 3}$	b) $\log_4 4 = x$ $\boxed{1 = x}$
c) $\log_3(x^2) = \log_3(x+12)$ $x^2 = x+12$ $-x -12 \quad -x -12$ $x^2 - x - 12 = 0$ $(x+3)(x-4) = 0$ $\boxed{x = -3 \mid x = 4}$	d) $\log_5(x+10) = 2$ $5^2 = x+10$ $25 = x+10$ $-10 \quad -10$ $\boxed{x = 15}$